

Cost-Effective Strategies for Infectious Diseases: A Multi-Objective Framework with Interactive Dashboard

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Abstract

During an infectious disease outbreak, policymakers must balance medical costs with social and economic burdens, seeking interventions that minimize both. To support this decision-making process, we developed a framework that integrates multi-objective optimization, cost-benefit analysis, and an interactive dashboard. This platform enables users to input cost parameters and immediately obtain a cost-optimal intervention strategy. As an example, we applied the framework to the early outbreak of COVID-19 in Korea. The results show that cost-optimal solutions for costs per infection ranging from 2,978 USD to 170K USD exhibited similar patterns. This highlights that once the cost per infection is specified, our approach generates the corresponding cost-optimal solution without additional calculations. Our framework supports decision-making by accounting for the trade-off between policy and infection costs. It delivers rapid optimization and cost-benefit analysis results, enabling timely and informed decision-making during critical phases of a pandemic.

Keywords: Infectious disease, Mathematical modeling, Multi-objective optimization,
Cost-benefit analysis, Dashboard

Introduction

During the COVID-19 pandemic, governments faced a trade-off problem between minimizing infections and the economic burden from non-pharmaceutical interventions, such as lockdowns and gathering restrictions [1]. Identifying an optimal strategy is challenging since multiple possible strategies may satisfy Pareto optimality according to health and economic costs [2–5]. Decision-makers face two central questions: (1) What is the best intervention strategy to minimize the costs of interventions and infections simultaneously? and (2) What are the reasonable costs of these interventions and infections? In this research, we answer these questions based on a research framework with an COVID-19 example.

In recent decades, increasing air travel and the growing concentration of populations in urban areas have accelerated the global spread of infectious diseases such as SARS, H1N1 influenza, MERS, and COVID-19 [6, 7]. Although traditional measures such as isolation, quarantine, and community containment were successfully implemented during the 2003 SARS outbreak [8], most countries were unable to control the spread of COVID-19 in 2020 using these standard measures [9]. These contrasting outcomes highlight the urgent need for more acceptable and cost-effective intervention strategies, particularly for emerging respiratory infectious diseases for which pharmaceutical interventions may not be immediately available [10].

Researchers have studied mathematical modeling, parameter estimation, optimization, and cost-benefit analysis for infectious diseases. Compartmental models [11, 12], stochastic models [13–15], agent-based models [16–19], and network models [20–22] are employed to capture the transmission dynamics of infectious diseases

and the interactions among individuals. Based on these modeling methods, optimization can identify the most effective non-pharmaceutical or pharmaceutical intervention strategy [23]. Optimal control theory has been utilized to determine time-varying non-pharmaceutical interventions (NPIs) that minimize a single objective, typically either disease burden or economic loss [24–27]. To minimize both infection and intervention costs simultaneously, multi-objective optimization is adopted, identifying Pareto-optimal strategies [28–32]. Note that single-objective optimization requires predefined weights or costs prior to the optimization process, whereas multi-objective optimization does not require such preset parameters in advance, thereby avoiding the need for extensive computational simulations repeatedly.

Since modeling and optimization results are theoretical, they need to be evaluated against actual costs and presented to users in a more accessible format. Cost-benefit analysis quantifies the efficiency of modeling or optimization results in various interventions during an epidemic of the disease. Paltiel et al. demonstrated that weekly testing is cost-effective under moderate transmission scenarios by comparing incremental cost-effectiveness ratios (ICER) to societal willingness-to-pay thresholds [33, 34]. Sandmann et al. evaluated the optimal timing of lockdowns that allowed for GDP losses of 2% to 15% per day [35], while Kohli et al. calculated ICER for vaccination campaigns in terms of averted infections and quality-adjusted life years [36]. To bridge the gap between complex modeling and policy practice, recent work has proposed multi-objective results. For example, a study presents a web tool to explore trade-offs in influenza control, but few platforms allow real-time adjustments of both epidemiological and economic parameters for emerging pathogens [37, 38]. Although many studies have analyzed infectious disease epidemics using the individual techniques mentioned, we developed a novel framework that synthesizes all of these methods into a single workflow. Research that simultaneously addresses both multi-objective optimization and cost-benefit analysis remains rare. Moreover, there is no

81 previous study that has translated such results into an intuitive dashboard that non-
82 specialists in mathematical modeling can immediately use. Our work, therefore, offers
83 a new approach that swiftly delivers modeling, optimization, and economic evalua-
84 tion insights to decision-makers in a familiar format during the urgent situation of an
85 epidemic or pandemic.

86 In this paper, we first introduce the research framework for general infectious dis-
87 eases. Next, we present an application to the early phase of COVID-19 in Korea, which
88 encompasses mathematical modeling, parameter estimation, multi-objective optimiza-
89 tion, cost-benefit analysis, and the development of an interactive dashboard. Our
90 contributions in this research are threefold. First, we propose a novel methodological
91 approach that applies multi-objective optimization to address the inherent trade-offs
92 in policy interventions, a strategy that can be generalized to other infectious dis-
93 eases beyond COVID-19. Second, we reveal that there are only a few cost-optimal
94 patterns of transmission reduction non-pharmaceutical intervention (NPI) strategies
95 according to the infection cost. Third, the interactive dashboard offers an intuitive
96 decision-support tool that streamlines the process of selecting and adapting optimal
97 intervention policies, emphasizing the benefits of multi-objective optimization.

98 Results

99 To support decision-making in the early phase of infectious disease outbreaks, we
100 developed a systematic research framework composed of five sequential processes, as
101 illustrated by the orange diamonds in Figure 1. The framework begins with mathemat-
102 ical modeling, where an appropriate infectious disease model is formulated to reflect
103 the characteristics of the outbreak. This model defines the disease compartments (e.g.,
104 susceptible, infected, recovered) and key parameters based on country-specific contexts
105 and anticipated public health interventions. Next, parameter estimation is conducted
106 to calibrate unknown parameters of the model using observed epidemiological data,

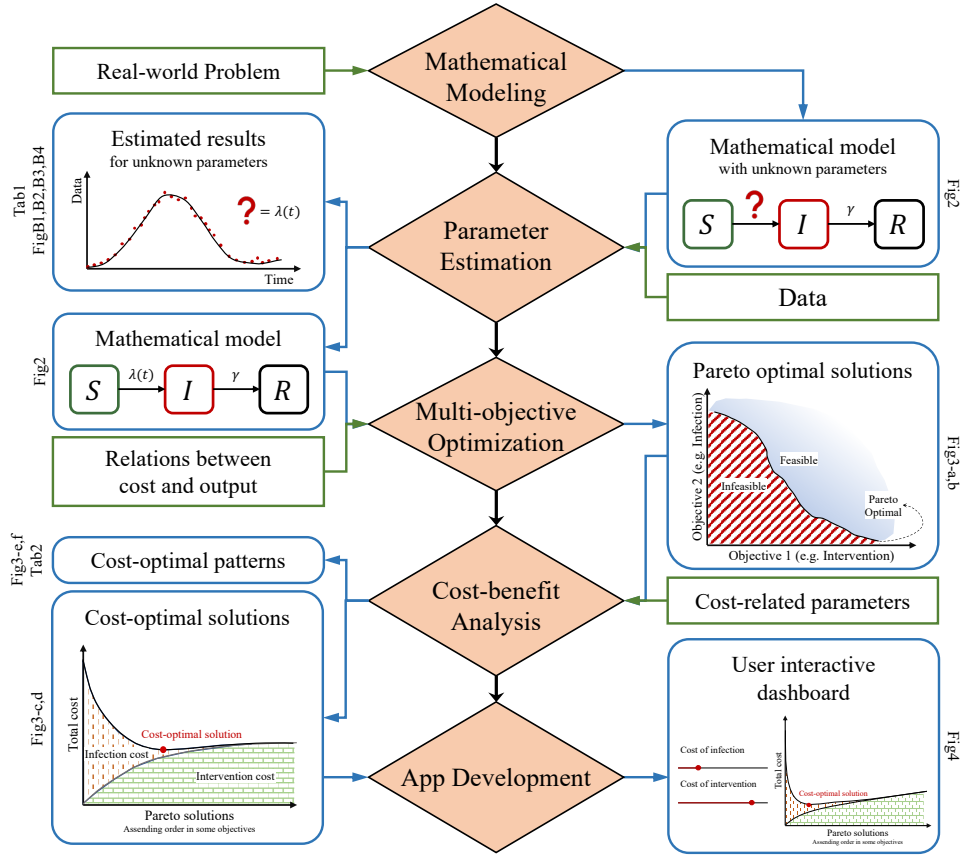


Fig. 1 Research framework for infectious diseases. Orange diamonds denote five steps of the framework, green rectangles represent required inputs, blue rounded rectangles summarize outputs with corresponding figures or tables.

107 such as case counts or hospitalization numbers. To enhance the robustness of this step,
 108 we performed sensitivity analysis and estimated the posterior distributions of param-
 109 eters using Bayesian inference, which allows the model to closely reproduce the actual
 110 epidemic or outbreak dynamics.

111 In the third step, multi-objective optimization is applied to identify Pareto-optimal
 112 intervention strategies that balance competing objectives—minimizing both the cost
 113 of infection and the cost of intervention. These trade-offs are quantified by defining
 114 objective functions that rely on the relationship between model outputs (e.g., the

number of infections) and practical cost metrics. Notably, changes in the relationship between cost and output lead to different sets of Pareto-optimal and cost-optimal solutions, as demonstrated in Appendix ???. Following this, cost-benefit analysis is employed to determine the most cost-effective intervention strategies based on pre-defined cost-related parameters. These parameters include, for example, the value of a statistical life, GDP loss due to lockdowns, quarantine costs, and fatality rates. These factors directly influence the selection of optimal strategies and can be adapted to reflect economic and societal differences across regions. Finally, we developed a web-based interactive dashboard to enable end-users—such as policymakers and public health officials—to explore and select intervention strategies based on their own cost assumptions and constraints. The dashboard provides real-time visualization of cost-optimal outcomes under various parameter settings, thereby offering actionable insights tailored to the user’s local context.

Throughout the framework, green boxes in Figure 1 indicate required inputs (e.g., real-world problem description, observational data, cost parameters), while blue boxes represent the results generated at each step of the process. This integrated framework thus provides a flexible and data-driven approach for guiding intervention decisions during infectious disease outbreaks. The following results are an application of the framework to the early phase of the COVID-19 pandemic in Korea. The objectives are to identify the optimal transmission reduction strategy that minimizes the cost of intervention and infection prior to vaccine development and to provide a dashboard that allows users to control the cost-related parameters.

Mathematical modeling

Figure 2 illustrates the Susceptible(S)-Exposed(E)-Infectious(I)-Isolated(Q)-Recovered(R)-Death(D) (SEIQRD) model to investigate the early phase of COVID-19 in Korea. There are five disease-related parameters (R_0 , κ , α , f , and γ): R_0 is the

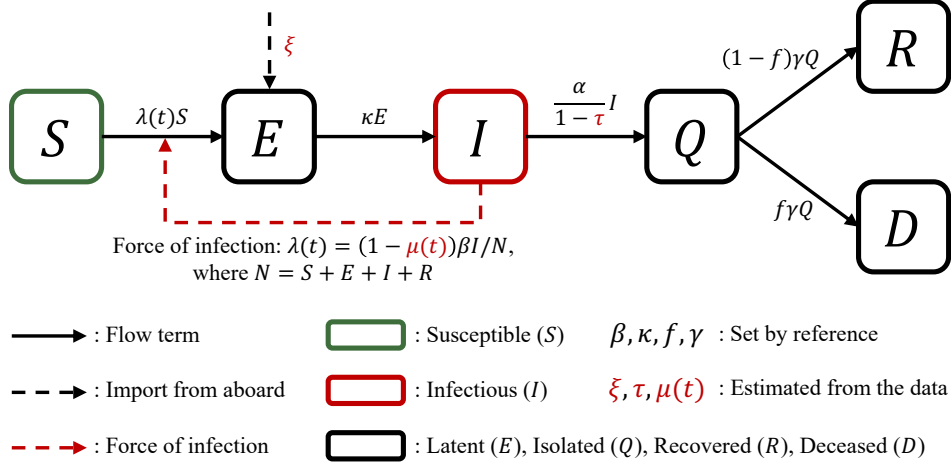


Fig. 2 Mathematical model for infectious diseases. The squares represent compartments of the mathematical model and the black arrows represent flows to the compartments. The black dashed arrow represents external importation which serves as a trigger for an epidemic. The red dashed arrow represents the force of infection which drives the spread of the disease in a country. The parameters in black and red are the disease-related and estimated parameters, respectively.

basic reproductive number of the disease, $1/\kappa$ is the average latent period, $1/\alpha$ is the average infectious period, f is the case fatality rate, and $1/\gamma$ is the average isolation period. There are three policy-related parameters ($\mu(t)$, ξ , and τ): $\mu(t)$ represents the transmission reduction by NPIs, ξ is the average number of imported cases per day, and τ is the average infectious period reduction by NPIs. The details of the mathematical model are presented in the Methods section.

Parameter estimation

Table 1 presents the parameters of the mathematical model. The parameters R_0 , $1/\kappa$, $1/\alpha$, and $1/\gamma$ are epidemiological quantities that characterize the disease and whose values can be obtained from a proper reference. However, $\mu(t)$, ξ , and τ may vary across countries or change over time depending on policies or interventions implemented during a given period. Therefore, it is necessary to estimate these unknown parameters and we utilized a hybrid parameter estimation scheme using two global

optimizers to obtain a posterior distribution: the Improved Multi-operator Differential Evolution (IMODE) and the Metropolis-Hastings (MH) algorithm [39], which is one of the Markov Chain Monte Carlo (MCMC) methods [40]. Table 1 shows the estimated values of the policy-related parameters obtained by fitting the model to the cumulative confirmed cases data. The average number of imported cases per day (ξ) is 0.2780, which is approximately 1 person per 4 days. The infectious period reduction (τ) is 62.18%, which means that contact tracing or testing policy reduces the infectious period by that value. The transmission reduction parameter, which has a value between 0 and 0.95, is estimated every two weeks since there were frequent changes in government transmission reduction policies. Note that μ is set to zero during the first two weeks, as confirmed cases were not yet detected. Appendix B presents the correlation between the estimated parameters derived from the MCMC chain.

Table 1 Parameter table for the SEIQRD mathematical model. The symbols, definitions, and values are presented in the table with corresponding references. $\mu(t)$, ξ , and τ are estimated from the cumulative confirmed data.

Symbol	Definition	Value	References
R_0	Basic reproductive number	2.87	[41]
$1/\kappa$	Average latent period	4 (day)	[42]
$1/\alpha$	Average infectious period	10 (day)	[43]
$1/\gamma$	Average isolation period	14 (day)	[44, 45]
f	Case fatality ratio	0.0173	[46]
$\mu(t)$	Transmission reduction by NPIs over time	[0~0.95]*	estimated
ξ	Average imported cases per day	0.3243* (person/day)	estimated
τ	Average infectious period reduction by NPIs	0.5836*	estimated

*: estimated parameter

Multi-objective optimization

Multi-objective optimization simultaneously minimizes multiple objectives without assigning explicit weights to each one. It identifies Pareto-optimal solutions, where no objective can be improved without compromising at least one of the others. In this work, we employ NSGA-II [47], a multi-objective genetic algorithm, to find Pareto solutions that minimize both infection and intervention costs at the same time. Figure 3(a)

172 illustrates the objective space, where the average effectiveness of transmission reduc-
173 tion and the number of infections are plotted on the x -axis and y -axis, respectively.
174 Note that each axis represents an objective functional of the multi-objective opti-
175 mization. Details of the multi-objective optimization are described in the Methods.
176 The black curve indicates the Pareto-optimal solutions obtained from more than a
177 thousand multi-objective optimization results. The colored circles represent Pareto
178 solutions from Strategy 1 (S1) to Strategy 5 (S5), corresponding to scenarios infect-
179 ing 10% to 0.001% of the population, respectively. The average transmission reduction
180 from S1 to S5 are 32.13%, 36.60%, 40.71%, 47.99%, and 58.32%, respectively. The red
181 diamond is estimated strategy (SE) have 53.05% of average transmission reduction
182 and 0.0279% of infected population, which is not on the Pareto curve.

183 Figure 3(b) shows the corresponding transmission reduction strategies of the
184 selected points in (a). The red curve is the estimated strategy (SE) obtained from the
185 data-fitting process. This curve corresponds to the red diamond in panel (a). Note
186 that every point in the Pareto curve in (a) corresponds to a strategy as in panel
187 (b). Strategies from S1 to S5 suggest strong intervention policies from 10th week to
188 2nd week since the detection of index case, respectively. As the average transmission
189 reduction increases, implementing strong policies earlier becomes more favorable. (SE
190 enhanced the transmission reduction from 6th week and it is similar timing with S3.
191 Strategy S5 suggests starting a strong policy in the 2nd week after detecting the index
192 case. However, results show that maintaining a prolonged and stringent intervention
193 without breaking is not recommended.

194 Cost-benefit analysis

Multi-objective optimization yields a set of Pareto-optimal solutions that simulta-
neously minimize intervention and infection costs, as illustrated in Figure 3(a,b).
However, because all Pareto solutions are optimal, no single solution can be deemed

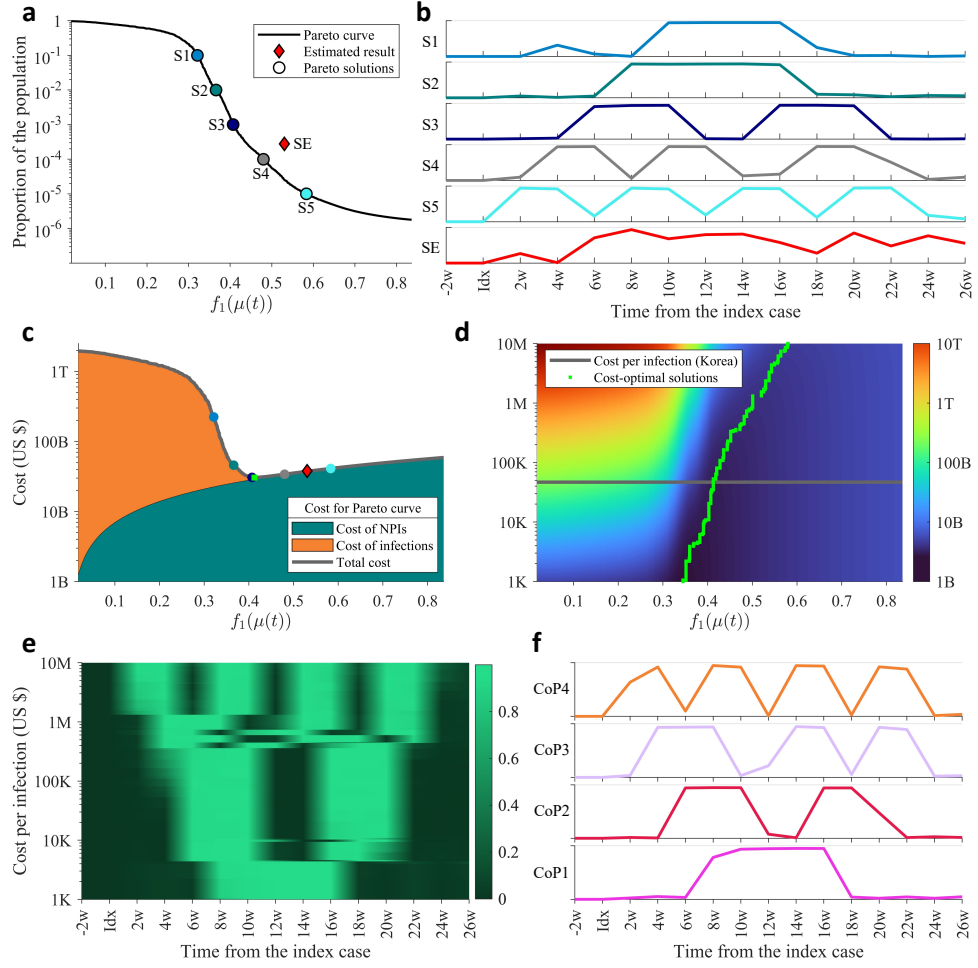


Fig. 3 Cost-benefit analysis results with Pareto solution. (a) Pareto curve and cost-optimal solution. The black solid line, colored circle, and red diamond represent Pareto curve, selected Pareto solution, and estimated point from data, respectively. (b) Corresponding solutions to the points in the panel (a). (c) Total costs of Pareto curve under cost-benefit analysis. Orange area, green area, and gray line represent infection cost, transmission reduction-related intervention cost, and total cost, respectively. (d) Total costs of Pareto curve with different cost per infection. The green points represent cost-optimal solutions with different cost per infection. The gray line corresponds to the panel (c). (e) Cost-optimal solutions for cost per infection. The line parallel to the x-axis represents the cost-optimal solution for the cost per infection and corresponds to the green points in the panel (d). (f) Cost-optimal policy for each cost per infection range.

superior without additional criteria. To address this, we compute the monetary costs of infection and intervention based on simulation results and the country's GDP. The

intervention cost for a strategy is computed as

$$C_{\text{int}}(\mu(t)) = C_1 f_1(\mu(t)) = C_1 \frac{\int_{t_0}^{t_f} \mu(t) dt}{t_f - t_0},$$

where C_1 is the maximum intervention cost in a day, $f_1(\mu(t))$ is the average reduction in relative intervention cost under $\mu(t)$. The infection cost for a strategy is computed as

$$C_{\text{inf}}(\mu(t)) = C_2 f_2(\mu(t)) = C_2 \int_{t_0}^{t_f} \mu(t) \mathcal{R}_0 \frac{\alpha}{1 - \tau} I(t) \frac{S(t)}{N(t)} dt,$$

where C_2 is the cost per infection and $f_2(\mu(t))$ is the total infection from t_0 to t_f under $\mu(t)$. The total cost denotes the sum of the intervention cost and infection cost $C_{\text{tot}} = C_{\text{int}} + C_{\text{inf}}$. Details of the cost-benefit analysis are described in the Methods section.

Since a single Pareto point corresponds to a single $f_1(\mu(t))$ value, the x -axis of Figure 3(c,d) corresponds to a Pareto solution. Figure 3(c) shows the cost-benefit analysis results where the cost per infection is set as 39213 USD and the maximum GDP reduction as 4.261%. The orange area represents the cost of infection, the green area represents the cost of transmission reduction intervention, and the gray curve represents the total cost of each strategy. The colored circles are Scenarios S1 to S5, and the red diamond is SE. The green square is the cost-optimal solution for the given cost per infection and intervention cost with an average transmission reduction value of 41.25% and total cost of 30.6B USD. The total costs for strategies S1 to S5, and SE are 223.6B, 45.8B, 30.7B, 34.0B, 41.1B, and 37.9B USD, respectively. The difference between the cost-optimal solution and SE is 7.3B USD and 11.79% in average transmission reduction. Note that if the government implements a weaker strategy than the cost-optimal solution, the total cost increases very rapidly.

Figure 3(d) presents the cost-optimal solution when the cost per infection is changed within the range [1K USD, 10M USD]. For example, if the government implements $f_1(\mu(t)) = 0.3$ strategy and the cost per infection is 10K USD, the expected total cost is 124B USD, according to the heatmap. For each cost per infection, we emphasize the cost-optimal solution as green squares. The gray line is when the cost per infection is 39213 USD, which corresponds to Figure 3(c). If the cost per infection is 1K USD and 10M USD, the total cost of the cost-optimal solution is 25.6B USD and 46.1B USD, respectively. The differences in total cost and average transmission reduction between these two cases are 20.5B USD and 0.2356, respectively. If $f_1(\mu(t)) = 0.3$, the range of total cost is [32.0B USD, 108T USD]. Otherwise, if $f_1(\mu(t)) = 0.5$, the range of total cost is [35.2B USD, 63.9B USD].

Among thousands of Pareto solutions, less than 100 solutions are cost-optimal solutions. Figure 3(e) represents the corresponding cost-optimal solutions according to cost per infection. This figure is an expansion of the green squares in Figure 3(d). The dark green color indicates a weak transmission reduction policy, while the light green color represents a strong transmission reduction policy. Several points of discontinuity can be observed in the cost-optimal solutions with respect to the cost per infection. The cost-optimal pattern (CoP) ranges from CoP1 to CoP3, which are cost-optimal within the intervals [1K,4.41K), [4.41K,361K), [361K,1.33M), and [1.33M,10M] USD, respectively. We note that the cost-optimal pattern for Korea follows CoP2, given that the cost per infection is 39.2K USD. 46.1192 38.9454 37.2855 28.0372 25.6182

Table 2 presents the CoPs corresponding to different ranges of costs per infection. Solutions within each CoP share similar characteristics in terms of the transmission reduction strategy, specifically, the number of intervention periods, the duration of strong interventions, and the start and end time of interventions. This table may guide decision makers in selecting a cost-optimal strategy based on their evaluation of infection and intervention costs.

Table 2 Cost-optimal pattern (CoP) from the index case for cost per infection.

Cost per infection (USD)	Scenario	Strategy pattern (week)				Total cost (USD)	Total infection
		Begin	Increase	Strong	Decrease		
1.33M –	CoP4	0	0–1, 6–7, 12–13, 18–19	2–3, 8–9, 14–15, 20–21	4–5, 10–11, 16–17, 22–23	38.96B – 46.12	0.00103% – 0.00338%
361K – 1.33M	CoP3	2	2–3, 10–13, 18–19	4–7, 14–15, 20–21	8–9, 16–17 22–23	38.96B – 37.29B	0.00338% – 0.00678%
4.41K – 361K	CoP2	4	4–5, 14–15	6–9, 16–17	10–11, 18–21	28.04B – 37.29B	0.00678% – 0.467%
– 4.41K	CoP1	6	6–7	8–15	16–17	25.62B – 28.04B	0.467% – 2.62%

User-interactive dashboard

Since intervention and infection costs are not only difficult to estimate but also vary widely across settings and individuals, we developed an [interactive dashboard](#) using Python Shiny that allows users to adjust cost-related parameters, including GDP, GDP reduction, value of a statistical life (VSL), and the fatality rate. Figure 4, a snapshot of our dashboard, shows the cost-related parameters that users can adjust accordingly. By default, the dashboard is initialized with characteristics of COVID-19 and estimated parameters derived from data of the Republic of Korea. Beneath the parameter adjustment panel, there are model simulation results based on the demography-related, disease-related, and policy-related parameters.

The results in the right panel are similar to the results in Figure 3. The primary difference between the results displayed in the dashboard and those reported in this paper is that the cost-optimal results can be changed by adjusting the cost-related parameters, the quarantine period, and the fatality rate. When users adjust these parameters, the cost-optimal results are updated immediately: the cost-optimal solution is indicated by a green circle, the cost-optimal strategy is represented by a green line, the cost per infection is depicted by a gray dotted line, and the cost-optimal pattern is marked by a non-blurred line. Finally, our dashboard enables policymakers

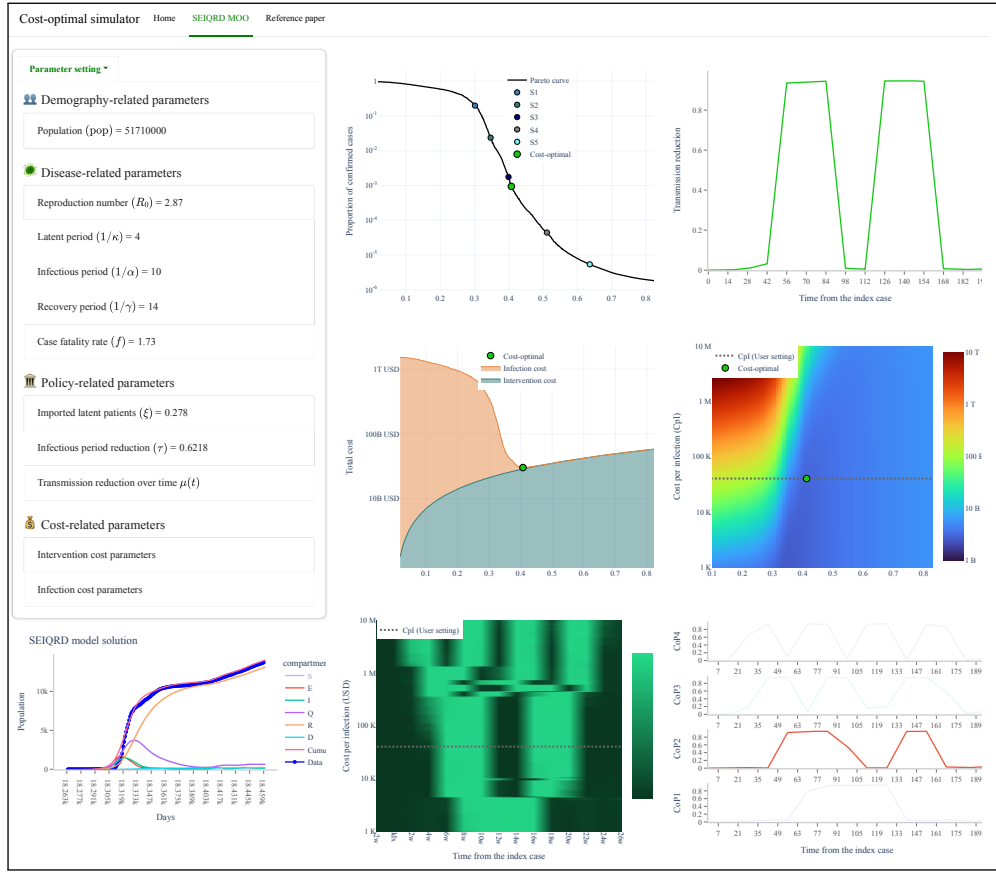


Fig. 4 Interactive dashboard The left panel features a slider bar that allows users to adjust cost-related inputs, while the right panel displays the corresponding simulation results along with a summary of the cost-benefit analysis.

257 to evaluate the cost-optimal solution based on their perspective immediately and to
 258 contextualize their plans by suggesting other possible cost-optimal options.

259 Discussion

260 The results presented offer retrospective insights into the COVID-19 pandemic in
 261 Korea. However, because the data are only used to estimate unknown parameters of an
 262 infectious disease model, the framework can be readily adapted for prospective appli-
 263 cations to support scientifically informed decision-making in future infectious disease

264 outbreaks, particularly in identifying cost-optimal intervention strategies. To apply the
265 framework to an emerging or unknown infectious disease, one needs to make informed
266 assumptions about the disease’s epidemiological characteristics, the country-specific
267 responses, and the functional relationship between model outputs and associated economic costs. Based on these assumptions, the framework can simulate the introduction
268 of the disease into a population via importation and identify Pareto-optimal and cost-
269 optimal intervention strategies. To obtain results for different infectious diseases, users
270 can modify the disease-related parameter using values from existing literature [48–50],
271 and then apply our framework. Similarly, to adapt the analysis to different countries,
272 users can adjust the population and policy-related parameters based on the data.
273 Since the policy-related parameters that capture the effects of interventions are estimated using a specific country’s data, cost-optimal solutions for other countries can
274 be similarly derived using their country’s respective data.
275
276

277 While the research framework makes it possible for policymakers to find a cost-
278 optimal solution under their cost-related parameter setting, the results derived from
279 this framework suggest that the relationship between the transmission reduction and
280 economic cost determines the cost-optimal intervention strategy. If the relationship is
281 linear as we have assumed in the main text, the cost-optimal solutions are on-off type,
282 indicating that the lockdown policy is more cost-effective than other strategies. This
283 supports the intervention strategy implemented in most countries. However, if mask-
284 wearing intervention is cheap and effective, and strong intervention is expensive and
285 ineffective, the early and constant intervention is more effective than other strategies.
286 This means that wearing masks and personal hygiene policies are more cost-effective
287 than the lockdown policy. Therefore, research on intervention cost is crucial as it
288 significantly influences the cost-optimal strategy to implement during an epidemic.

289 In this research, we only considered controlling transmission-related interventions
290 to obtain a Pareto optimal solution. However, optimal strategies on quarantine and
291 testing are also important to assess during a pandemic [44, 45].

292 Although our proposed framework provides a way to analyze cost-free and cost-
293 optimal intervention strategies, there are limitations to its practical implementation.
294 First, we adopted the established SEIQR model, which allows for rapid experimenta-
295 tion and generation of results. While the framework emphasizes structural design, it
296 remains flexible. Users can readily incorporate more complex models [51], without the
297 need for algebraic derivations, due to the implementation of the metaheuristic algo-
298 rithm [39, 47]. Second, if users wish to change the model, the objective functions, or
299 certain parameters, they can obtain different Pareto solutions. Appendix ?? suggests
300 that we can observe a similar cost-optimal pattern under different simulation settings.
301 Additionally, as long as users calculate the Pareto solutions, they can only change
302 the cost-related parameters to obtain a user-defined cost-optimal solution. Third, the
303 theoretical solution does not provide specific policies to achieve the suggested trans-
304 mission reduction value. Policymakers should refer to other papers on the relationship
305 between transmission reduction and specific policies [52–54]. Lastly, we considered
306 only the cost of infection without accounting for medical resources or potential over-
307 burdening, and detailed costs of other interventions such as limitations in gathering,
308 quarantine, testing, and other interventions. Nevertheless, the user can modify the cost
309 of intervention or infection to account for additional intervention or infection costs by
310 adjusting these costs to obtain corresponding cost-optimal solutions.

311 We formulate the mathematical model considering the importation of infected peo-
312 ple from abroad, transmission reduction, and infectious period reduction, which are
313 related to intervention policies during the early phase of a pandemic. Since the effect
314 of interventions is not known, these parameters are estimated using the parameter
315 estimation method, utilizing the hybrid method of a machine learning-based global

316 optimization (IMODE) and the statistical optimization method (MCMC). Using the
 317 mathematical model with estimated parameters, multi-objective optimization obtains
 318 Pareto solutions of the transmission reduction policy that simultaneously minimizes
 319 the cost of intervention and the cost of infection. Thereafter, cost-benefit analysis
 320 determines the cost-optimal solution among the Pareto solutions for a cost per infec-
 321 tion; e.g., the higher the cost per infection, the stronger the cost-optimal intervention.
 322 Since the cost-optimal solution is changed by the cost of interventions or infection,
 323 we build a web-based dashboard that enables customizing the cost and obtaining the
 324 corresponding cost-optimal strategy. This research framework can be applied to other
 325 respiratory infectious diseases at the beginning of a pandemic.

326 **Methods**

327 **Mathematical Modeling**

328 To describe the transmission dynamics of the early phase of the COVID-19 pandemic
 329 in Korea, we propose an extended SEIQRD compartmental model. The population
 330 is divided into six epidemiological compartments: Susceptible individuals (S) have no
 331 immunity and have not yet been exposed to the disease. Latent or exposed individuals
 332 (E) have been exposed to the disease but are not yet infectious. Infectious individuals
 333 (I) have become infectious and can transmit the disease to susceptible individuals.
 334 Isolated individuals (Q) have been identified and isolated due to self-reporting or
 335 contact tracing. Recovered individuals (R) have recovered from the disease and are
 336 assumed to be immune. Deceased individuals (D) have died from the disease.

337 The governing equations (1–6) represent the changes in each compartment.

$$\frac{dS}{dt} = -\lambda(t)S, \quad (1)$$

$$\frac{dE}{dt} = \lambda(t)S - \kappa E + \xi, \quad (2)$$

$$\frac{dI}{dt} = \kappa E - \frac{\alpha}{1-\tau} I, \quad (3)$$

$$\frac{dQ}{dt} = \frac{\alpha}{1-\tau} I - \gamma Q, \quad (4)$$

$$\frac{dR}{dt} = (1-f)\gamma Q, \quad (5)$$

$$\frac{dD}{dt} = f\gamma Q, \quad (6)$$

where $\lambda(t) = (1-\mu(t))\mathcal{R}_0\frac{\alpha}{1-\tau}I/N$ is the force of infection, \mathcal{R}_0 is the basic reproduction number, $1/\alpha$ is the average infectious period, τ is the infectious period reduction due to testing or contact tracing policies, $\mu(t)$ is the time-dependent transmission reduction resulting from policy interventions, and $N = S+E+I+R$. The parameter $\mu(t)$ consists of a set of values μ_i , each representing the level of transmission reduction during a specific period. The index i corresponds to the period starting on day $14 \times (i-1)$ from the beginning of the simulation, with each period spanning two weeks. The details on $\mu(t)$ are described in Appendix A. The parameter ξ is the average daily imported cases to the country; $1/\kappa$ is the mean latent period, that is, the average time to be infectious from the infection; $1/\gamma$ is the average removal period, that is, the average time to recover or die from the disease since isolation; and f is the fatality rate, that is, the probability of death among infected cases. Note that the infectious period does not begin with the onset of symptoms, but rather with the start of infectiousness. For example, patients infected by COVID-19 can be infectious two days before symptoms appear [55]. Figure 2 represents the flowchart of the model.

Data-fitting Process

We utilize two global optimizers—Improved Multi-operator Differential Evolution (IMODE) and Markov Chain Monte Carlo (MCMC)—to estimate the parameters [39, 40, 56]. IMODE achieved first place in the Congress on Evolutionary Computation (CEC) 2020 competition on bounded single-objective optimization algorithms.

358 It combines the advantages of global and local search, focusing on exploration at the
 359 beginning and exploitation at the end of the optimization process. IMODE excels
 360 at finding optimal solutions for given function evaluations within a specified domain
 361 without a preset initial point. We employ IMODE to minimize the difference between
 362 model simulation results and the cumulative confirmed cases data (C_{data}).

$$\min_{\theta} \int_{t_0}^{t_{end}} \left\| \frac{\alpha}{1-\tau} I(t; \theta) - C_{data} \right\|_2 dt \quad (7)$$

363 where $\theta \in \{\xi, \tau, \mu(t)\}$ are the policy-related parameters.

364 Sensitivity analysis

365 The sensitivity analysis results show the relative impact of each parameter on the
 366 model outputs. It can provide information on which parameter may effectively control
 367 the outputs or which parameter can be ignored. We performed Partial Rank Coefficient
 368 Correlation (PRCC) analysis on the number of infected cases and confirmed cases to
 369 assess the sensitivity of the parameters to these model outputs. Note that the confirmed
 370 cases are an output for the parameter estimation and the infected cases are an output
 371 for the multi-objective optimization. μ and τ are the most sensitive parameters for both
 372 outputs among the policy-related parameters, where those parameters affect disease-
 373 related parameters β and α . The PRCC results are presented in the Appendix C.

374 Multi-objective optimization

375 We assume that interventions affecting the infectious period and the number of
 376 imported cases during an epidemic remain fixed, as these are largely determined by
 377 a country's health or medical system. In the multi-objective optimization, we focus
 378 solely on changes in the transmission reduction parameter $\mu(t)$, which is influenced
 379 by government policies such as mask-wearing, social distancing, and gathering restric-
 380 tions. The goals of the optimization are to simultaneously minimize both infection

381 levels and the costs associated with transmission-related interventions by adjusting
 382 $\mu(t)$. Since $\mu(t)$ represents time-dependent transmission reduction and the expression
 383 $\int_{t_0}^{t_f} \mu(t) \mathcal{R}_0 \alpha (1 - \tau) I(t) \frac{S(t)}{N(t)} dt$ reflects the total number of infections over the simula-
 384 tion period, the two objectives correspond to intervention stringency and epidemic
 385 size, respectively. However, directly quantifying the relationship between $\mu(t)$ and the
 386 cost of the intervention is difficult. To address this, we assume that the cost of inter-
 387 vention is proportional to both its effectiveness and stringency. Similarly, the cost of
 388 infection is assumed to be proportional to the total number of infections. Hence, we
 389 minimize the functions $f_1(\mu(t))$ and $f_2(\mu(t))$ represented by

$$\arg \min_{\mu(t)} \begin{bmatrix} f_1(\mu(t)) \\ f_2(\mu(t)) \end{bmatrix} = \arg \min_{\mu(t)} \begin{bmatrix} \frac{\int_{t_0}^{t_f} \mu(t) dt}{t_f - t_0} \\ \int_{t_0}^{t_f} \mu(t) \mathcal{R}_0 \alpha I(t) \frac{S(t)}{N(t)} dt \end{bmatrix}. \quad (8)$$

390 Note that f_1 and f_2 are proportional to the monetary cost but do not exactly equal
 391 the cost. The multi-objective optimization problem simultaneously minimizes f_1 and
 392 f_2 where the governing equations are given by equation ((1)–(6)).

393 The multi-objective optimization will find solutions near the Pareto curve, that is, a
 394 set of Pareto solutions in the objective plane composed of the codomain of f_1 and f_2 . A
 395 solution is considered Pareto-optimal if it is not dominated by any other solution; that
 396 is, no other solution performs better in at least one objective without performing worse
 397 in at least one other objective. We obtained the Pareto curve using the built-in function
 398 *multiobjga* that employs the non-dominated sorting genetic algorithm II (NSGA-II)
 399 in MATLAB [47]. To get an accurate solution, we independently run *multiobjga* one
 400 thousand times and assembled the Pareto solution by finding the Pareto front.

401 **Cost-Benefit Analysis**

402 Since the Pareto solutions are outputs and not costs, we introduce C_1 as the maximum
 403 intervention cost in a day and C_2 as the cost per infection, to convert the outputs into

monetary costs. We consider C_1 to be proportional to two factors: the GDP per capita of the country and the reduction of the GDP by intervention. The GDP of the Republic of Korea in 2019 is 31902, and the maximum reduction is assumed to be 4.26% based on the difference between the GDP projection by OECD in 2019 and the real GDP data [57, 58]. C_2 is divided into the average hospitalization cost and expected cost of death [34–36, 59, 60]. The following are the formulas used for C_1 and C_2 :

$$C_1 = \text{GDP} \times \text{GDP}_{\text{MaxRed}} \quad (9)$$

$$C_2 = C_H + f \times \text{VSL}, \quad (10)$$

where GDP is total GDP of the country, $\text{GDP}_{\text{MaxRed}}$ is the maximum GDP reduction by transmission reduction intervention, C_H is the average hospitalization cost per infection, f is case fatality rate, and VSL is the value of statistical life. Details of the cost-benefit analysis are described in the Appendix.

Dashboard

The parameters in equations C_1 and C_2 are difficult to specify as single fixed values. For example, VSL can change according to average age, wage, income elasticities, and ethical considerations [61–65]. To address this variability, we developed a dashboard that enables users to select their own cost-related parameters and obtain cost-optimal results within seconds. We built the web dashboard using the Shiny package in Python and included both a mathematical model simulator and a [cost-optimal intervention policy simulator](#). In the mathematical model simulator, users can change various parameters of the SEIQRD model and check the simulation results immediately. In the cost-optimal intervention policy simulator, users can adjust the five economic-related

parameters, which are inputs to the costs C_1 and C_2 . This real-time optimization simulator is possible because the multi-objective optimization does not require a weight parameter for each objective.

Supplementary information.

Declarations

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Data and material availability

All the data, confirmed cases, death cases are uploaded in the Github. The dashboard can be accessible via <https://jongmin-lee.shinyapps.io/demomookorea/>.

Code availability

The results can be generated by the attached code in Github https://github.com/ljm1729-scholar/MOO_framework.

Author contribution

- Funding
- Conflict of interest/Competing interests (check journal-specific guidelines for which heading to use)
- Ethics approval and consent to participate

446 • Consent for publication

447 If any of the sections are not relevant to your manuscript, please include the heading

448 and write 'Not applicable' for that section.

449 **Appendix A Transmission reduction $\mu(t)$**

450 The time-dependent transmission reduction function $\mu(t)$ is defined using linear
451 interpolation of μ_i , that is, the transmission reduction at time $t = i \times 14$:

$$\mu(t) = \mu_{n+1} - \left(n - \frac{t}{14}\right) (\mu_{n+1} - \mu_n), \quad (\text{A1})$$

452 where $n = \lceil \frac{t}{14} \rceil$ and $\mu_0 = 0$. Note that we assume transmission reduction changes every
453 two weeks, in accordance with government announcements regarding adjustments in
454 intervention strategies. We also assume that testing and controlling of imported cases
455 are implemented by the government. The parameter ξ represents the mean daily
456 imported cases per day. The imported cases are affected by the screening system in the
457 airports or borders. We assume that there are no infected cases at the beginning of the
458 simulation since the spread of infectious diseases are triggered by imported cases. The
459 parameter τ represents the infectious period reduction that is affected by the testing
460 or tracing system of the government. We estimated these policy-related parameters
461 from the confirmed cases data.

462 **Appendix B Hybrid parameter estimation**

463 To reduce computational time and find a more accurate solution, we utilized two
464 algorithms – the global optimization algorithm named improved multi-operator dif-
465 ferential evolution (IMODE) and the Markov-chain Monte Carlo (MCMC) method.
466 In our simulations, we used the cumulative confirmed cases data and minimized the
467 L_2 -norm between the data and the corresponding output from the simulation results.
468 We estimated the policy-related parameters $\xi, \tau, \mu_3, \mu_4, \dots$ as described in the main
469 text. IMODE finds the optimal solution faster and the MCMC provides the solution
470 with posterior information.

471 B.1 Improved multi-operator differential evolution

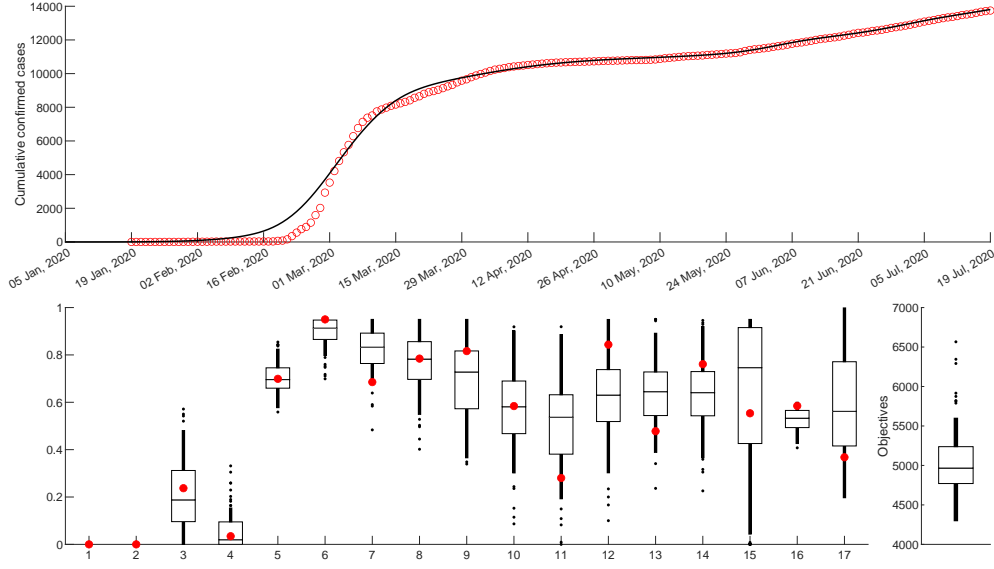


Fig. B1 IMODE estimation results. (A) shows the cumulative confirmed cases and simulation results. (B) shows the 25 estimation results with boxchart and the best estimation results with red circle point. (C) shows the L2-norm of 25 estimation results.

472 If a local optimizer is used, user-specified initial values must often be taken into
 473 account, since the solution may be sensitive to the starting point. The use of a global
 474 optimizer eliminates this problem since it does not require an initial value for the
 475 optimization. To reduce the randomness of the global optimizer, we run IMODE
 476 twenty-five times and select the best solution among them [39]. Each simulation termi-
 477 nates after 100,000 function evaluations. Figure B1 shows the estimation results. Since
 478 the IMODE algorithm can search for the most suitable solution in the loss landscape,
 479 we used the IMODE results as prior information in the MCMC process.

480 B.2 MCMC process

481 We use the MATLAB package to run the Markov-chain Monte-Carlo (MCMC) algo-
 482 rithm [40, 56]. This package requires the parameter list, prior distribution of the

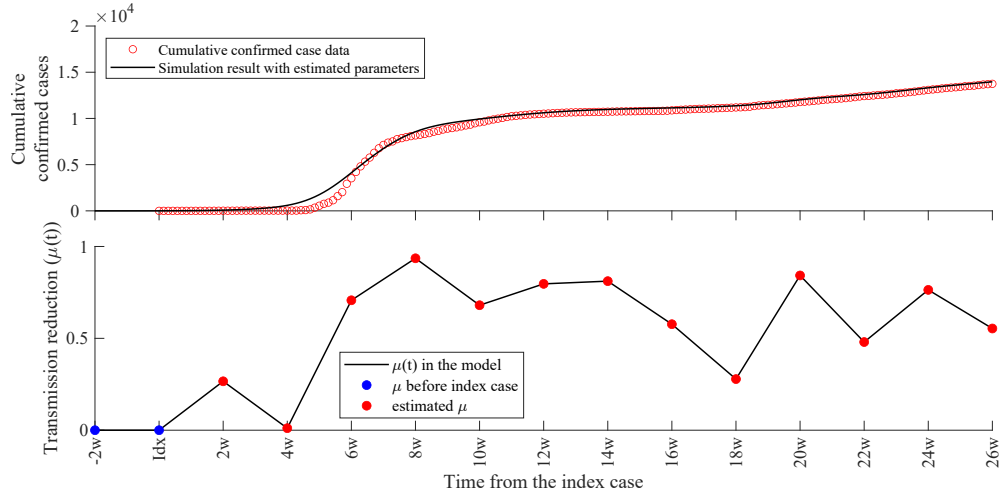


Fig. B2 MCMC estimation results. (A) shows the cumulative confirmed cases and simulation results. (B) show the estimated $\mu(t)$. (C) shows the daily confirmed cases and simulation results.

parameters, the equations of the system, and the objective function of the MCMC process. The package uses the delayed-rejection adaptive metropolis (DRAM) algorithm [56] to search for the posterior distribution. We set the prior distribution as a normal distribution that has a mean value from the IMODE results and a standard deviation of 0.05. Figure B2 shows the parameter estimation results.

Figure B3 presents the MCMC chains obtained from the DRAM algorithm. The total length of the chain is 1 million, where the burn-in period is half of the total chain length. The red lines indicate the burn-in period, and the rest of the chain composes the posterior distribution.

Figure B4 presents the correlation between the estimated parameters derived from the MCMC chain. Many of the elements have correlation values lower than 0.5 except for the diagonal part. The lower correlation values indicate the practical identifiability of the estimated parameters.

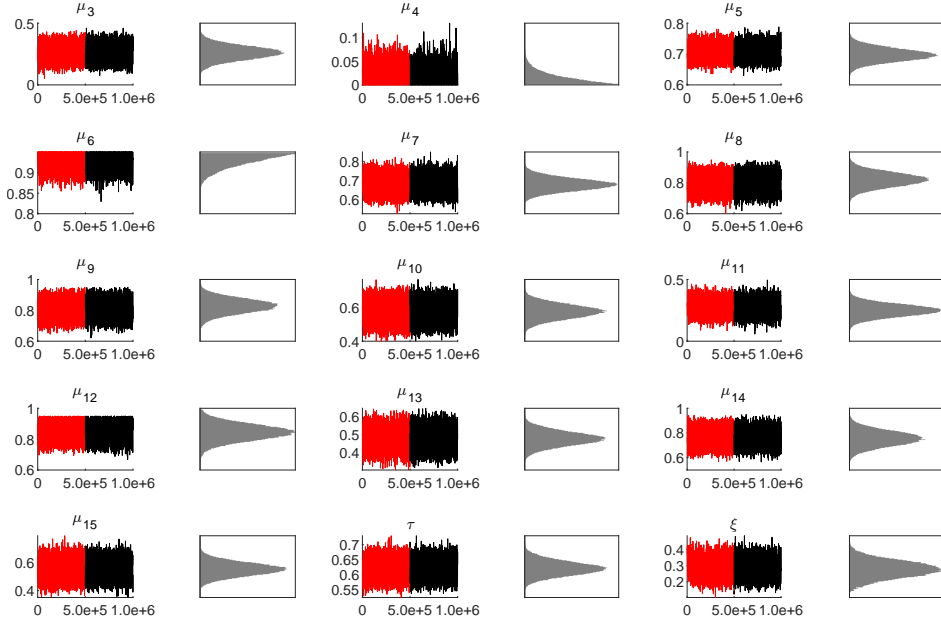


Fig. B3 MCMC chain for the estimated parameters. The red period indicate the burn-in that is half of the total iteration. The black period composes the posterior distribution

Appendix C Sensitivity analysis results

Sensitivity analysis presents how impactful the parameters are on the simulation results. We set μ as constant in this sensitivity analysis simulation. We check the sensitivity for two outputs – cumulative confirmed cases and the number of infections. The cumulative cases are used for the data-fitting process and the number of infections is used for the multi-objective optimization. Figure C5 presents the PRCC results for two outputs. The β has the highest correlation and is larger than 0.8 for all time. κ and ξ have 0.6723 and 0.6203 at the beginning of the simulation but they monotonically reduce to 0.2432 and 0.0837, respectively. τ is 0.5 at the beginning of the simulation but the correlation keeps increasing up to 0.8.

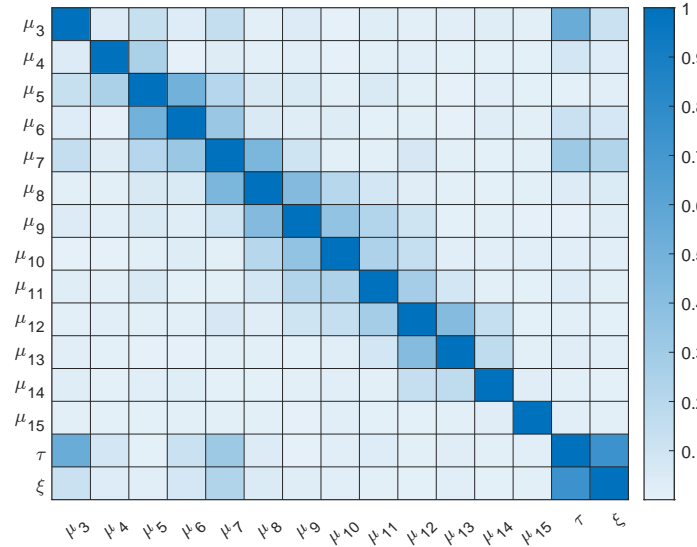


Fig. B4 Correlation between the estimated parameters. The white color indicate the lower correlation and blue color indicate the higher correlation.

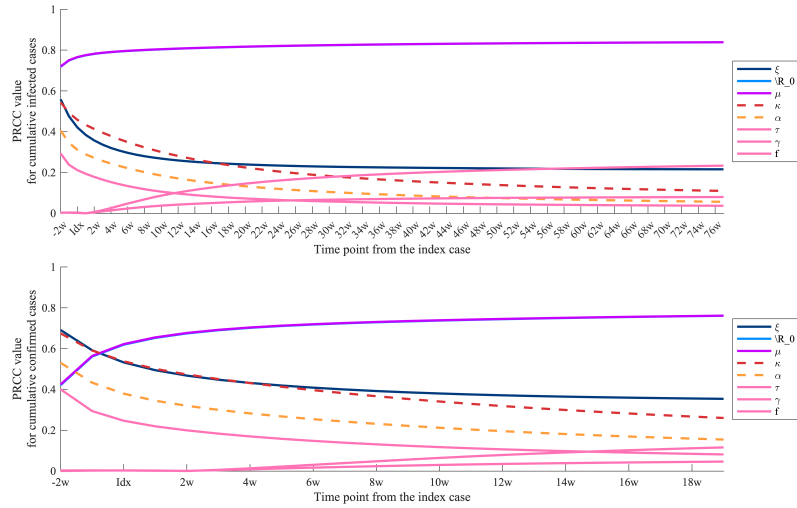


Fig. C5 Parameter estimation results. Correlation between the model simulation and parameter over time. Solid and dashed line indicate positive and negative correlation, respectively.

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